

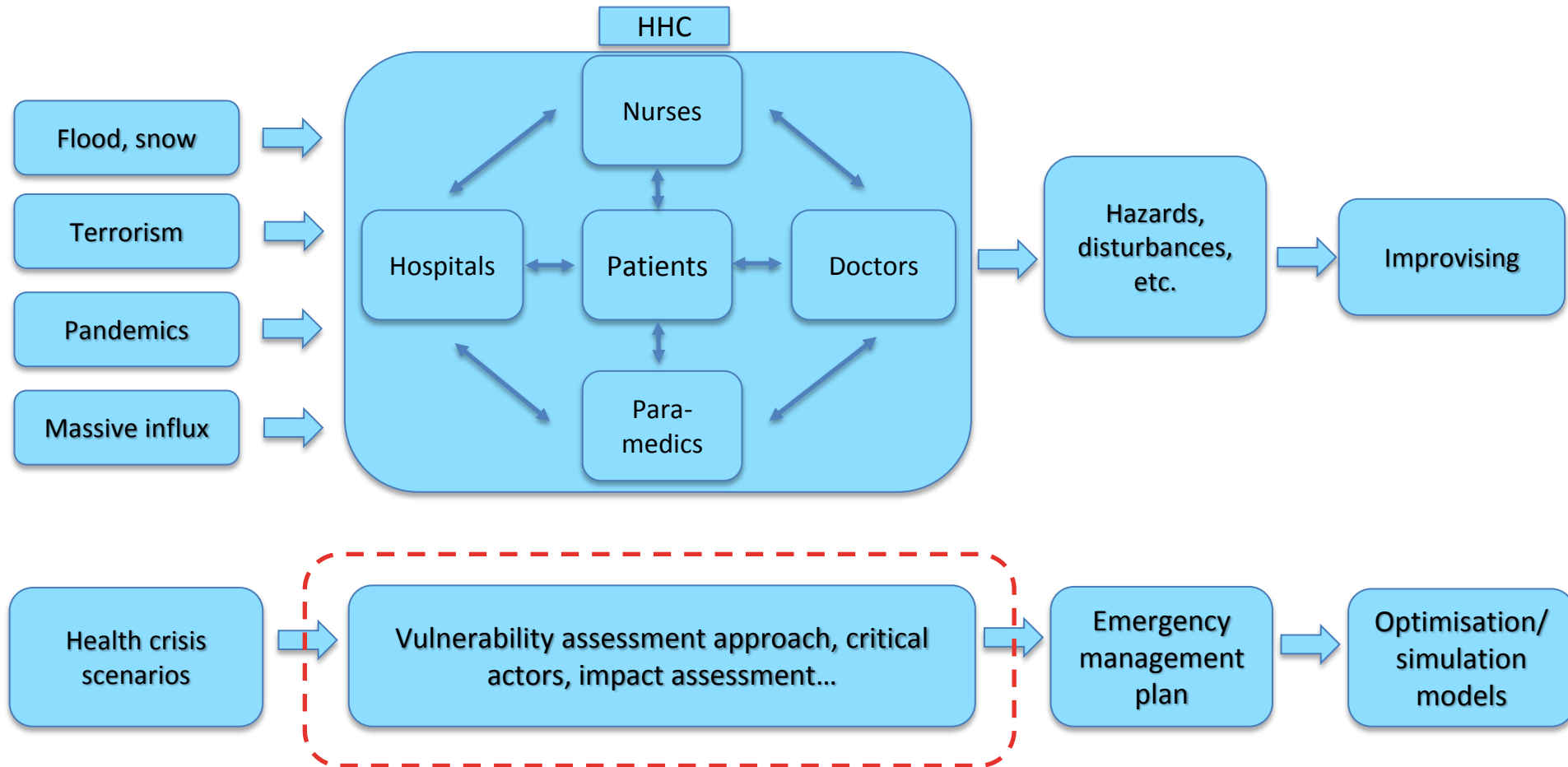
“Home Health Care vulnerability assessment using graph theory and matrix methods”

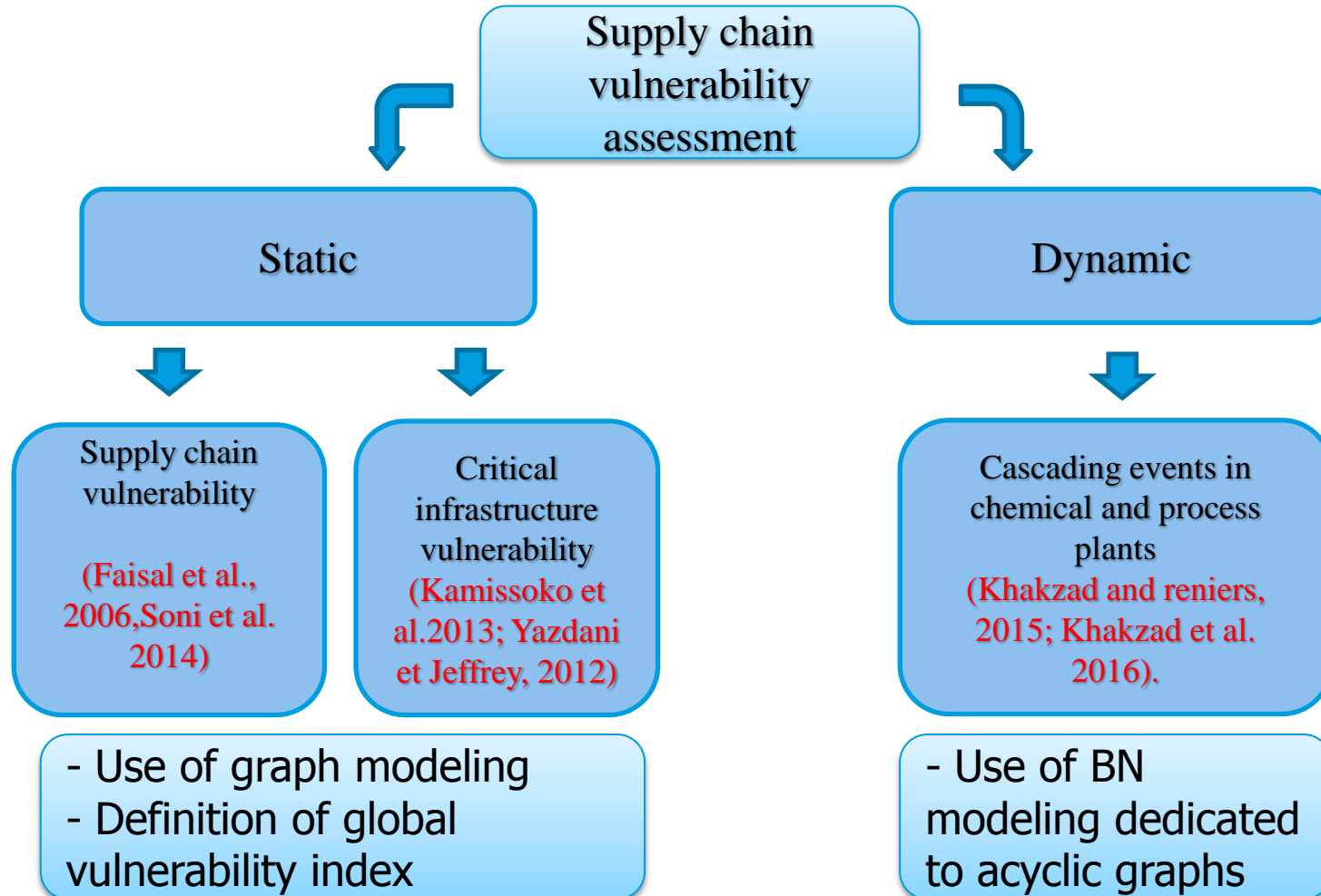


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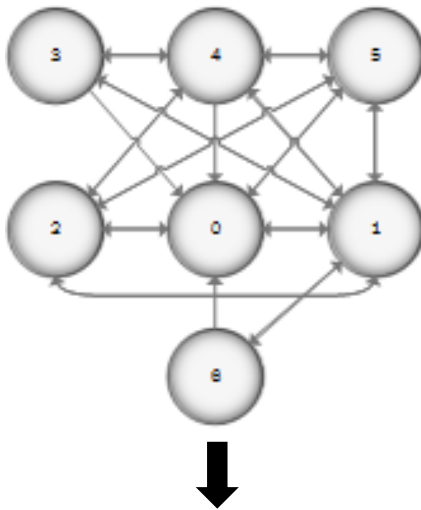
- Context
- State of the art
- Vulnerability assessment approach
- Prospects





- Define a set of criteria for vulnerability assessment of each actor and flow facing different types of crisis.
- Provide indexes to assess the vulnerability of actors and flows based on actor resilience and flow robustness, using matrix operations that do not necessitate a big computational effort.
- Propose a method to calculate the dynamic vulnerability that takes into account the cascading events in a cyclic graph.

- 1- Digraph modelling:



$$F = \begin{pmatrix} 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 & 1 & 1 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

N°	Acteur
0	Patients
1	Call centre
2	Nurses
3	Deliverers
4	Doctors
5	Hospitals
6	Collectors

2- Influence matrix:

Rule: « The more the flow is important for the actor (flow consumer), the more its degradation/breakdown has more probability to disrupt the functioning of this actor and the higher the associated value is. »

Verbal judgment	Assigned value (a_{ij})
No importance	0
Very weak	1
Weak	2
Medium	3
Strong	4
Very strong	5



Actors	0	1	2	3	4	5	6
0	0	4	4	0	0	3	0
1	3	2	3	4	4	3	3
2	5	4	2	0	3	2	0
3	4	3	0	1	0	0	0
4	3	4	4	0	2	2	0
5	3	3	2	0	3	1	0
6	1	3	0	0	0	0	1
Total	19	23	15	5	12	11	4



$$wf_{ij} = \frac{a_{ij}}{\sum_{l=0}^6 a_{il}} ; i, j = 0 \dots 6$$

$$WF = \begin{pmatrix} 0 & 0.173 & 0.266 & 0 & 0 & 0.272 & 0 \\ 0.157 & 0.086 & 0.200 & 0.800 & 0.333 & 0.272 & 0.75 \\ 0.263 & 0.173 & 0.133 & 0 & 0.250 & 0.181 & 0 \\ 0.210 & 0.130 & 0 & 0.200 & 0 & 0 & 0 \\ 0.157 & 0.173 & 0.266 & 0 & 0.166 & 0.181 & 0 \\ 0.157 & 0.130 & 0.133 & 0 & 0.250 & 0.090 & 0 \\ 0.052 & 0.130 & 0 & 0 & 0 & 0 & 0.25 \end{pmatrix}$$



■ 3- Actors' resilience

- Example: measure of P (qualitative)

- **P = 1**: nominal state, without crisis.

- **1 < P < 2**: the actor is more or less prepared to manage the disturbance (the value 2 can be seen as a threshold).

- **P = 3**: the actor is not prepared at all to manage the disturbance, he/she will improvise.

$$LRS(i,i) = IC(i) * P(i) * R(i) \quad LRS = \begin{pmatrix} LRS(1,1) & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & LRS(6,6) \end{pmatrix}$$

■ 4- Flows' robustness

- Robustness: the robustness is the ability to maintain the operations intact while undergoing disruptions (Kamissoko et al. 2013).

➤ Criteria: Lack of quality (Q), Cost (C), Delay (D).

Exemple: Measure of « D »

- D_0 : Standard duration of flow delivery, without delay;

- D_1 : Duration of flow delivery in times of crisis;

- $DL = D_1 - D_0$: Delay

- $ADL = (D_1 - D_0)_{\text{acceptable}}$: Acceptable delay (threshold),

$$D = \begin{cases} 1, & \text{if } R_D < 1; \\ R_D, & \text{if } 1 \leq R_D \leq 2: \text{ acceptable delay;} \\ 3, & \text{if } R_D > 2: \text{ above the acceptable threshold;} \end{cases}$$

$$\longrightarrow R_D = 1 + \frac{DL}{ADL}$$

$$D = \begin{pmatrix} 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 3 & 3 & 3 & 3 & 3 & 3 & 3 \\ 3 & 3 & 3 & 0 & 3 & 3 & 0 \\ 3 & 1 & 0 & 3 & 0 & 0 & 0 \\ 2 & 3 & 3 & 0 & 3 & 3 & 0 \\ 3 & 3 & 3 & 0 & 3 & 3 & 0 \\ 2 & 1 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

■ 5- Vulnerability assessment

- Vulnerability : vulnerability is the incapacity of a stake to resist to the occurrence of a feared event and to recover efficiently its nominal function during a given period of time (Kamissoko et al. 2013).

❖ Flows vulnerability:

$$FVI(i, j) = LRS(i, i) * LRB(i, j); i, j = 0 \dots 6$$

$$FVI = \begin{pmatrix} LRS(1,1) & \dots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \dots & LRS(6,6) \end{pmatrix} * \begin{pmatrix} LRB(1,1) & \dots & LRB(1,6) \\ \vdots & \ddots & \vdots \\ LRB(6,1) & \dots & LRB(6,6) \end{pmatrix}$$

❖ Actors vulnerability

$$AVI(j) = \sum_{i=0}^6 w_{ij} * FVI(i, j); j = 0 \dots 6$$

■ 6- Dynamic vulnerability assessment

❖ A period (p) is the laps of time required for all flows to circulate once in the network.

■ Initialization

$$DFVI(i, j, 1) = FVI(i, j); i, j = 0 \dots 6;$$

$$DAVI(i, 1) = AVI(i); i = 0 \dots 6;$$

■ Dynamic Flow Vulnerability Index

$$DFVI(i, j, p + 1) = DAVI(i, p) * FVI(i, j); i, j = 0 \dots 6;$$

■ Dynamic Actor Vulnerability Index

$$DAVI(i, p + 1) = \sum_{j=0}^{j=6} wf_{ji} * DAVI(j, p) * FVI(j, i); i, j = 0 \dots 6;$$

■ 7- Actors classification

❖ Vulnerability Priority Index (VPI)

$$VPI(i, p) = \frac{DAVI(i, p)}{\sum_{j=0}^{j=6} DAVI(j, p)}; i = 0 \dots 6;$$

Période	P=1			P=2		
Indice	DAVI	VPI	Rang	DAVI	VPI	Rang
0	31.181	0.155	3	834.004	0.177	2
1	19.286	0.096	7	504.878	0.107	7
2	23.084	0.115	6	569.553	0.121	4
3	37.440	0.187	1	840.908	0.178	1
4	34.935	0.174	2	803.306	0.170	3
5	23.860	0.119	5	556.528	0.118	5
6	30.182	0.150	4	595.349	0.126	6

- Establish a criteria Weighting (AHP),
- Define classes of actors (critical, influential, dependent, neutral),
- Define mitigation strategies according the actors' classes,
- Define a “redesign” of the HHC supply chain aiming at minimizing the overall vulnerability of the structure.

Thank you!

Do you have any questions?